

1 **Large Contribution of Kilometer-Scale Snow Transport to Alpine Hydrology Constrained**
2 **by Differentiable Modeling and Airborne Lidar**

3 **E. N. Boardman^{1,2}**

4 ¹Graduate Program of Hydrologic Sciences, University of Nevada, Reno, Reno, NV, USA

5 ²Mountain Hydrology LLC, Reno, NV, USA

6 Corresponding author: Elijah N. Boardman (eli.boardman@mountainhydrology.com)

7 **Key Points:**

- 8 • A differentiable model of snow transport constrains the minimum seasonal flux required
9 to explain lidar-based snow accumulation patterns.
- 10 • Extensive deep snow accumulation (3-9 times local snowfall, >0.01 km²) requires mass-
11 weighted mean contributing distances of 0.3 to 2.1 km.
- 12 • Interbasin snow transport can double the catchment area of first-order streams and can
13 contribute 7% of water yield at the 100 km² scale.
14

15 **Abstract**

16 The farther you roll a snowball, the more snow is accumulated. How far must you roll a
17 snowball to create a major alpine snow drift? From this analogy, I develop a framework using
18 airborne lidar data and differentiable modeling to constrain the minimum seasonal transport
19 flux needed to explain alpine snow accumulation patterns. In the Wind River Range, Wyoming,
20 100 m grid cells with 3-6 m SWE must accumulate snowfall over mass-weighted mean
21 contributing distances of 0.3 to 2.1 km, and upwind source areas can exceed 3 km². Interbasin
22 snow transport augments local snowfall by at least 23% in a first-order stream catchment (2
23 km²), with the upwind “snowshed” doubling the effective catchment area. Snow imported
24 across topographic divides is equivalent to 7% of annual streamflow in a 125 km² watershed.
25 Kilometer-scale snow transport mediates alpine hydrology by permitting deep drift formation
26 and augmenting the catchment water balance.

27 **Plain Language Summary**

28 Deep snow drifts represent a large amount of water concentrated into a small area, in contrast
29 to precipitation, which is spatially smoother. Wind and avalanches can transport snow in
30 mountain environments, concentrating relatively homogeneous snowfall into deep drifts.
31 Snowfall must be accumulated over a relatively large area, and travel a long distance, to
32 account for the amount of water stored in deep snow accumulation zones. I estimate a lower
33 bound on snow transport with a new method that combines machine learning, snow modeling,
34 and remote sensing. The results show that snowfall must accumulate over several kilometers to
35 create observed drift patterns. Additionally, large amounts of snow can blow across mountain
36 ridges, which has the effect of importing extra precipitation into downwind watersheds.

37

38 **1 Introduction**

39 Mountain snowpacks are a global water resource (Viviroli et al., 2007; Li et al., 2017),
40 and the spatial distribution of snow mediates streamflow, soil moisture, and ecohydrology
41 (Luce et al., 1998; Litaor et al., 2008; Williams et al., 2009; Wigmore & Molotch, 2024).
42 Snowpack patterns are notoriously challenging to quantify (Dozier et al., 2016) due to process
43 complexity (e.g., wind turbulence: Musselman et al., 2015) and the 10^8 range of relevant scales
44 (Sturm, 2015).

45 Processes controlling the deposition and redistribution of alpine snow (Figure 1) are
46 intensely studied at the scale of individual ridges and small catchments (e.g., Hiemstra et al.,
47 2006; Lehning et al., 2008; Farinotti et al., 2010; Mott et al., 2010; Naaïm-Bouvet et al., 2010;
48 Mott et al., 2014; Walter et al., 2020). However, the scale-emergent effects of snow transport
49 are more newly explored (Marsh et al., 2024; Quéno et al., 2024). Landscape-scale simulations
50 commonly assume sub-kilometer fetch distances with suspension capped ~ 5 m above ground
51 (Pomeroy et al., 1993; Marsh et al., 2020a). However, some regions exhibit multi-kilometer
52 fetch distances (Figure 1A) with snow plumes extending hundreds of meters (Figure 1B). Some
53 models can produce plumes (Groot Zwaaftink et al., 2011), but the attendant high-resolution
54 wind fields complicate large-scale applications (Mott & Lehning, 2010; Schneiderbauer &
55 Prokop 2011). Most models do not track snow, with the exception of Lagrangian particle
56 tracking of preferential deposition (Wang & Huang, 2016).

57 The contributing distances and source areas of snow drifts have been studied for
58 decades (Adok, 1977), but typically not in alpine environments. Early snow fence studies
59 suggest contributing distances of ~ 1 -3 km (Komarov, 1954; Tabler, 1971). From semi-empirical
60 sublimation equations, Tabler and Schmidt (1973) infer a transport limit of 457-1421 m,
61 sensitive to wind speed (assumed 12 m/s) and particle size. Snow accumulated from extensive
62 alpine plateaus clearly contributes to “drift glaciers” (Olyphant, 1985; Hoffman et al., 2007;
63 McGrath, 2022). Outcalt and MacPhail (1965) estimate that a ~ 0.1 km² drift glacier could collect
64 snow from a ~ 1.3 km² source area by visual delimitation of topography and treeline. However,
65 few if any studies have attempted to map drift source areas in comparable environments over
66 the past 60 years.

67 Novel methods are needed to learn from patterns in remotely sensed snow data
68 (Dozier, 2011; Sturm, 2015). I leverage differentiable modeling (Shen et al., 2023) to learn the
69 fraction of snow exported from grid cells to their downwind neighbors (Figure 1). By tracking
70 snow parcels through the trained model, I address two questions: (1) what contributing
71 distances and source areas are necessary to explain alpine snow accumulation patterns, and (2)
72 how might snow transport across topographic divides influence the catchment water balance?

78 **2 Methodology**

79 In a three-part framework (Figure S2), I first estimate local snowfall and net
80 accumulation with remote sensing and a process-based model. Second, I constrain snow
81 transport by learning export fractions between grid cells. Third, I track snow parcels through
82 the transport model.

83 2.1 Study Area and Data

84 I demonstrate this method in the Wind River Range, Wyoming (WRR). Anderson (2002)
85 uses the WRR as the type locality for alpine plateau surfaces, a feature of mountain ranges
86 globally (Calvet et al., 2015). Multi-kilometer wind fetch distances on these summit plateaus
87 (Figure 1A) can produce deep drifts that mediate glaciation and streamflow (Boardman et al., in
88 prep.).

89 Airborne lidar and hyperspectral data were acquired in the WRR on May 31, 2024, by
90 Airborne Snow Observatories (ASO: Painter et al., 2016) in conjunction with backcountry
91 fieldwork to constrain density variations (Boardman et al., in prep.). The final snow water
92 equivalent (SWE) map is aggregated to 100 m resolution to highlight landscape-scale patterns,
93 and an area outside lidar coverage is imputed (Figure S1, analogous to Appendix B of Boardman
94 et al., in prep.).

95 2.2 Snow Modeling

96 The lidar-based “reference SWE map” reflects accumulation as well as patterns of
97 interception, melt, and sublimation. A simple snow mass and energy balance model such as the
98 two-layer snowpack sub-model of the Distributed Hydrology Soil Vegetation Model (DHSVM)
99 can account for many of these processes and estimate seasonal accumulation (Wigmosta et al.,
100 1994).

101 2.2.1 Setup and Calibration

102 DHSVM land surface parameters are from LANDFIRE (2022) and RCMAP (Rigge et al.,
103 2021). Meteorological data from gridMET (Abatzoglou, 2013) are disaggregated with MetSim
104 (Bennett et al., 2020). Modeled snowfall is distributed in proportion to the reference SWE map
105 or uniformly below the lidar snowline. This multiplier-based approach implicitly accounts for
106 preferential deposition and redistribution (Jackson, 1994; Vögeli et al., 2016).

107 Parameters are based on Sun et al. (2019) and refined by calibration, along with
108 temperature and precipitation biases. Four objectives constrain model behavior: SWE root
109 mean square error (RMSE); SWE R^2 for cells with SWE >1 m; SWE volume bias; and albedo
110 RMSE for cells with SWE >0.1 m (from ASO hyperspectral data). Calibration is implemented
111 using multi-objective Bayesian optimization (Emmerich et al., 2008).

112 The selected parameter set has SWE $R^2 = 0.991$ for cells with SWE >1 m. Exceptional
113 model skill is possible because the reference SWE pattern is used to distribute snowfall. The
114 calibrated model is Pareto-efficient across objectives (SWE RMSE = 0.12 m, volume bias =
115 +8.8%, albedo RMSE = 0.26).

116 2.2.2 Snowfall and Accumulation

117 I estimate net accumulation by accounting for ablation in the lidar-based SWE map:
 118 “reference accumulation” = reference SWE + (modeled accumulation – modeled SWE). DHSVM
 119 indicates maximum SWE around May 10-15, 2024, with a 3% reduction by the May 31 survey,
 120 so the adjustment between SWE and seasonal accumulation is minor.

121 I model local snowfall in DHSVM assuming a smoother precipitation distribution.
 122 Orographic effects and preferential deposition control alpine snowfall (Lehning et al., 2008,
 123 Mott et al., 2018) at scales below the 4 km resolution of gridMET data. I infer a plausible above-
 124 ground snowfall pattern with a 2 km moving-average of the lidar-based pattern, applied twice
 125 to remove edge artifacts. The 2 km kernel preserves mountain-scale patterns while removing
 126 drifts. A smaller window preserves obvious drift patterns, which is disallowed. I also test three
 127 alternative patterns: (1) a 4 km moving-average, (2) Lanczos spline interpolation of gridMET
 128 precipitation, and (3) a uniform distribution. The 2 km kernel preserves the most spatial
 129 heterogeneity, so I use this snowfall pattern to estimate a lower bound on required transport
 130 and test sensitivity with the other patterns.

131 2.3 Differentiable Snow Transport Model

132 I develop a differentiable model of snow transport based on a feed-forward neural
 133 network, or NN (Caterini & Chang, 2018). Mass conservation and flux continuity are enforced.
 134 Unlike typical “black box” NN applications, learned weights physically represent the fraction of
 135 available snow exported from each grid cell (Figure 1).

136 2.3.1 Mathematical Structure

137 Assume an (x, y) model grid, size (m, n), with the prevailing wind direction toward
 138 increasing x. Each grid cell corresponds to a single neuron (Figure S2), with m “layers” (map
 139 columns) each containing n “neurons” (grid cells). Equation 1 defines transport:

$$140 \quad A_x = W_x A_{x-1} + b_x = \begin{bmatrix} w_{1,1}^x & \cdots & w_{1,n}^x \\ \vdots & \ddots & \vdots \\ w_{n,1}^x & \cdots & w_{n,n}^x \end{bmatrix} \begin{bmatrix} a_1^{x-1} \\ \vdots \\ a_n^{x-1} \end{bmatrix} + \begin{bmatrix} b_1^x \\ \vdots \\ b_n^x \end{bmatrix} \quad (1)$$

141 The linear activation (A_x) represents the total available mass from local snowfall and
 142 incoming transport. First and last layer activations are zero to enforce no-transport boundaries.
 143 The bias (b_x) defines the local snowfall, and the weights matrix (W_x) defines the fraction of A_x
 144 transported between layers x-1 and x. Weights are scaled so that the export fraction (F_x)
 145 preserves mass:

$$146 \quad F_x = \sum_i w_{i,j}^{x+1}, \quad 0 \leq F_x < 1 \quad (2)$$

147 To enforce flux continuity, only tridiagonal entries of W_x are nonzero, so that snow from
 148 (x, y) can only arrive at (x+1, y) and (x+1, y±1). Dispersion occurs when snow is split between
 149 two downwind cells.

150 Only one of $w_{j+1,j}^x$ or $w_{j-1,j}^x$ may be significantly nonzero, thereby encoding a center-of-
 151 mass (COM) deflection angle at each cell. Following Figure S3, the maximum COM deflection
 152 angle (θ_{max}) is constrained by the ratio between lateral and diagonal transfer fractions:

$$153 \quad w_{j\pm 1,j}^x \leq w_{j,j}^x * \frac{\tan(\theta_{max})}{1 - \tan(\theta_{max})} \quad (3)$$

154 The mass flux (Q_x) is defined by A_x and F_x , where \odot denotes element-wise
 155 multiplication:

$$156 \quad Q_x = F_x \odot A_x = W_x A_x \quad (4)$$

157 The net accumulation (N_x) is the residual of A_x and Q_x :

$$158 \quad N_x = (A_x - Q_x) = (1 - F_x) \odot A_x \quad (5)$$

159 The distance-weighted mass flux (Q_{dist}) is analogous to the mean of Q_x , except that
 160 diagonal transport is scaled by $\sqrt{2}$ using distance matrix D :

$$161 \quad Q_{dist} = \frac{1}{n * m} \sum_{x,y} (D \odot W_x) A_x \quad (6)$$

162 2.3.2 Training

163 The network learns transport pathways between the modeled above-ground snowfall
 164 and reference ground accumulation patterns. The reference accumulation pattern defines the
 165 sole training example, and the NN is not intended for generalized prediction since W_x encodes
 166 the site-specific spatial arrangement of scour and deposition zones. An error tolerance is
 167 required relative to the reference accumulation pattern due to uncertainty in the modeled
 168 snowfall.

169 The transport flux is equifinal, e.g., snow imported to (x, y) could come from $(x-1, y)$ or
 170 $(x-2, y)$, but a lower bound on transport can be estimated by minimizing Q_{dist} . Energy is
 171 dissipated roughly in proportion to distance traveled per unit mass (i.e., from friction), so
 172 minimizing Q_{dist} implies a lower bound on energy available for transport. Individual particles
 173 might follow longer paths, but minimizing Q_{dist} constrains the “path of least resistance”
 174 between local snowfall and net accumulation patterns.

175 2.3.3 Implementation

176 At 100 m resolution, the 442 km² study area requires 260 NN layers, each with 170
 177 neurons. Prevailing westerly winds in the WRR are naturally oriented to the grid; elsewhere, a
 178 rotation may be necessary. The COM deflection angle is constrained to $\pm 22.5^\circ$, consistent with
 179 drift patterns observed in the snow lidar data. With three valid weights per neuron, the NN has
 180 132,090 learnable parameters (last layer fixed to zero).

181 Three constraints define an error tolerance, subject to which Q_{dist} is minimized. The
 182 predicted accumulation pattern must have RMSE < 8 cm, which is the lowest error tolerance
 183 that does not cause unphysical aberrations (e.g., overfitting causes unrealistically high transport
 184 in forested areas). To reduce spatial biases, the error of each cell may not exceed 200% of the

185 overall RMSE, i.e., ± 16 cm. To reduce depth-dependent biases, cells are binned by accumulation
186 depth in 10 cm increments, and the mean absolute bias across all bins may not exceed 1 cm.

187 Training is implemented in PyTorch (Paszke et al., 2019) using automatic differentiation
188 (Baydin et al., 2017) and the Adam optimizer (Kingma & Ba, 2017) for 10^5 iterations. Training
189 takes ~ 1.5 days on a consumer GPU.

190 2.4 Parcel Tracking

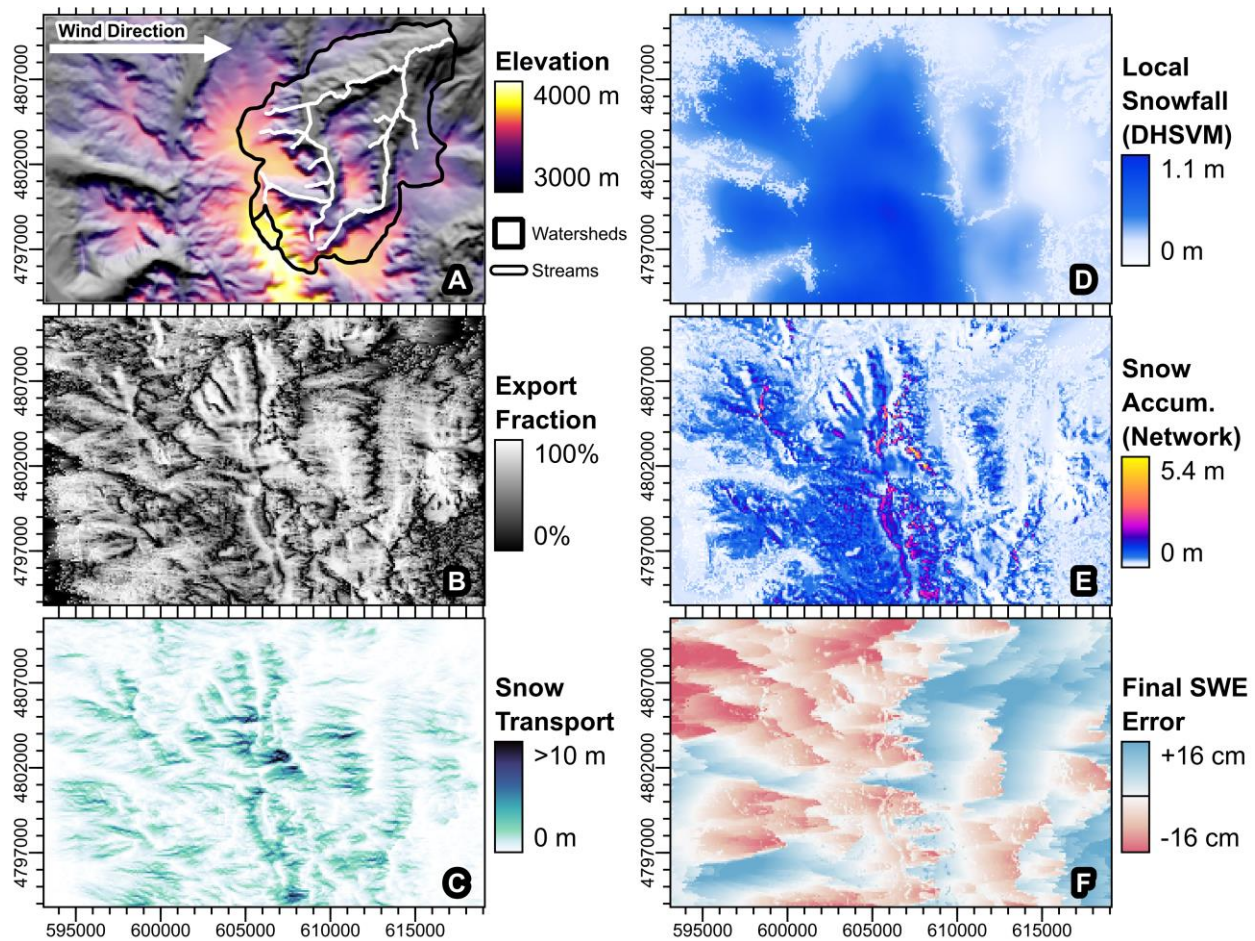
191 Mobile snow (Q_x) is assumed to be well-mixed within each cell. However, the total
192 available snow (A_x) is not necessarily well-mixed, since transport may occur above a relatively
193 immobile ground snowpack. To estimate a lower bound on transport, I assume that local
194 snowfall contributes as much as possible of the net accumulation in each cell (Figure S4).

195 For each cell with net export (snowfall > accumulation), I propagate its contribution
196 through the NN and track its contribution to all downwind cells. I then calculate the mean mass-
197 weighted contributing distance of net accumulation in each cell (including local snowfall with
198 zero distance). I also calculate the fraction of accumulation originating within a given upwind
199 distance and the number of upwind cells that contribute at least 1, 10, or 100 mm of their local
200 snowfall to a given downwind cell. Finally, I track how much snowfall from each cell ends up
201 within specific watershed masks.
202

203 **3 Results and Discussion**

204 **3.1 Snow Transport Flux**

205 Figure 2 illustrates the northern WRR study area. The modeled 2024 seasonal snowfall is
 206 0.42 m averaged across the domain, reaching 1.1 m at high elevations. Very deep accumulation
 207 zones (3-5.4 m SWE) contain 3-9 times more water than the local snowfall at those locations.
 208 The minimized distance-weighted mass flux is 0.91 m SWE per grid cell (Q_{dist} , Eq. 6), slightly
 209 higher than the mean flux of 0.80 m (Q_x , Eq. 4) due to diagonal transport. Q_x can reach 8-14 m
 210 at downwind plateau margins. Note that Q_x represents transport over an entire accumulation
 211 season, not an instantaneous flux.



212
 213 **Figure 2.** Study area maps: (A) shaded relief colored by elevation; (B) export fraction, F_x ; (C)
 214 transport flux, Q_x ; (D) local snowfall modeled by DHSVM, b_x ; (E) net snow accumulation from
 215 the neural network, N_x ; (F) error in final modeled SWE relative to measurements.

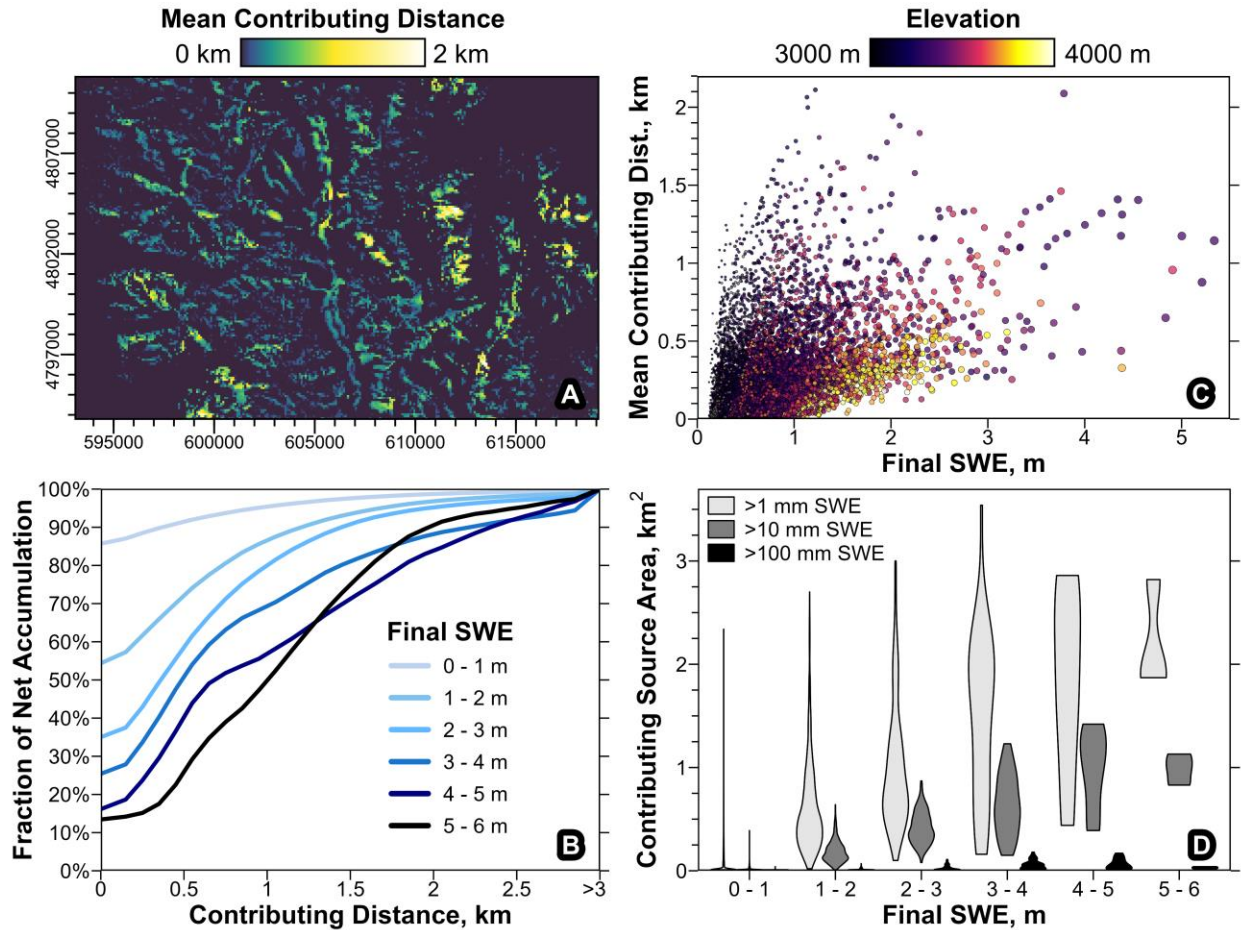
216 Higher export fractions (F_x , Eq. 2) are associated with summit plateaus, and lower export
 217 fractions define sheltered areas (Figure 2B). The median upwind shelter angle (Winstral &
 218 Marks 2002) is 2° for cells that export at least 0.5 m of SWE, and 15° , 20° , or 29° for cells that
 219 import at least 0.5, 1, or 2 m of SWE. Based on the WindNinja Reynolds-Averaged Navier-Stokes
 220 solver (Wagenbrenner et al., 2019), the median transport flux is 0.42 m in areas with lower-
 221 quartile wind speeds and 0.72 m (71% higher) in areas with upper-quartile wind speeds (Figure

222 S5). Despite lacking any explicit process representation or topographic input data, the NN
223 implies sensible relationships between terrain, wind, and snow transport.

224 After accounting for ablation effects (Section 2.2.2), the NN matches the reference SWE
225 map with $R^2 = 0.96$. Residual errors appear related to missing orographic effects and blowing
226 snow sublimation (Figure 2F). Since errors are constrained to ± 16 cm with no depth-dependent
227 bias (Section 2.3.3), these errors should minimally impact analysis of the seasonal flux into cells
228 with SWE > 1 m. Indeed, by minimizing Q_{dist} , spatial biases in the residual error have the effect
229 of underestimating transport, a desirable property for the lower bound estimated here.

230 3.2 Contributing Distance and Source Areas

231 The mass-weighted mean contributing distance over the whole study area is 0.15 km,
232 increasing to 0.43 km for cells with SWE > 1 m and 0.92 km for SWE > 3 m (Figure 3A). Local
233 snowfall exceeds net accumulation for 86% of cells with SWE < 1 m. However, cells with SWE > 1
234 m import 46% of their net accumulation, and the upwind contributing distance increases
235 rapidly for deep drift zones (Figure 3B). The fraction of net accumulation imported from > 1 km
236 upwind increases from 14% for cells with 1-2 m SWE to 21%, 32%, 44%, and 53% for
237 successively deeper SWE bins (1 m increments). For 100 m cells with 4-6 m SWE ($N = 13$), 47%
238 of net accumulation is imported from > 1 km upwind, and 15% is from > 2 km upwind.



239

240 **Figure 3.** (A) Map of mass-weighted mean contributing distance; (B) fraction of net
 241 accumulation that originates within a given distance upwind, binned by final SWE; (C) final SWE
 242 vs. mean contributing distance for each grid cell, colored by elevation; (D) distribution of
 243 contributing source areas from which at least 1, 10, or 100 mm of local snowfall is imported to
 244 a given downwind cell, binned by final downwind SWE.

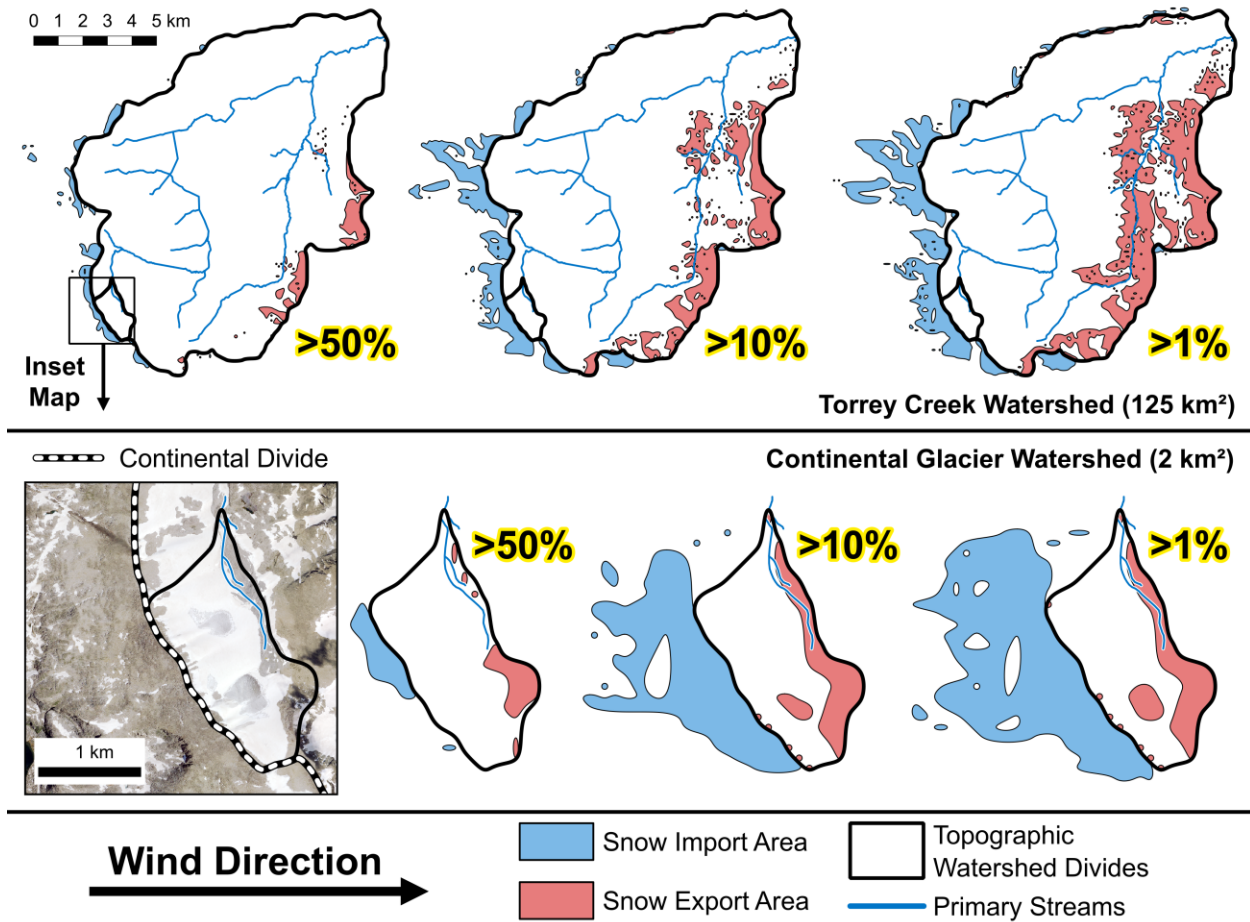
245 The relationship between contributing distance and final SWE depth is nuanced (Figure
 246 3C), with Pearson correlation $r = 0.59$. The mean contributing distance varies from 0.3 to 2.1 km
 247 for SWE >3 m. Drifts covering a larger area require longer contributing distances compared to
 248 isolated drifts. Long-distance transport is also associated with deep snow at relatively low
 249 elevations due to reduced local snowfall. For example, there is an $r = -0.41$ correlation between
 250 elevation and contributing distance for cells with 1-2 m SWE. The longest mean contributing
 251 distances (1.9-2.1 km) are associated with relatively low elevations (3200-3400 m) and medium
 252 to deep SWE (1-4 m) along the downwind margins of summit plateaus.

253 Most deep snow is accumulated incrementally from a relatively large source area
 254 (Figure 3D). Two notable cirques collect snowfall from 2.8-3.5 km² contributing source areas.
 255 The median source area contributing at least 1 mm of SWE to a given downwind cell is 0.9 km²
 256 for downwind cells with SWE >2 m and 1.8 km² for SWE >3 m. Source areas shrink when raising
 257 the minimum contribution threshold, with a median of 1.8, 0.7, or 0.04 km² contributing >1,
 258 >10, or >100 mm to cells with SWE >3 m. There is a negative correlation ($r = -0.76$, $N = 49$)

259 between the size of areas contributing >1 or >100 mm to cells with SWE >3 m. Concentrated
260 transport (>100 mm imported from each cell in a >0.1 km² area) produces deep accumulation
261 (2.8-4.8 m SWE) with an abnormally low mean contributing distance of 0.41 km, compared to
262 0.83 km across all cells in the same accumulation range. The topographic setting of these
263 concentrated transport areas (steep headwalls) suggests a dominant role of avalanches. The
264 stratification of concentrated and dispersed source areas might help classify dominant snow
265 transport processes.

266 3.3 Snowshed Boundaries

267 Snow transport across topographic divides complicates the concept of catchment area.
268 Two streams are gauged in the study area: Torrey Creek (125 km²), monitored continuously by
269 the author, and a meltwater stream from the upper Continental Glacier (2.0 km²), monitored
270 intermittently by Vandeberg and VanLooy (2016, 2024). Figure 4 illustrates the “snowshed”
271 boundaries of these streams, defined here as the area from which some fraction of snowfall
272 may contribute to streamflow at a specified pour point. Snowsheds overlap between
273 watersheds because import/export areas also retain some local snowfall. Moreover, snowsheds
274 are spatially discontinuous due to intervening sheltered areas (i.e., snow may blow over a
275 sheltered gully).



276

277 **Figure 4.** “Snowshed” boundaries for the Torrey Creek and Continental Glacier watersheds
 278 (locations in Figure 2A). Colored polygons represent areas where at least 50%, 10%, or 8% of
 279 the local snowfall is imported into or exported out of the watershed. Imagery: NAIP, July 2022.

280 The effective Torrey Creek catchment increases by 16 km² (13%) when including areas
 281 that contribute >1% of local snowfall. Conversely, an interior area of 23 km² (18%) exports >1%
 282 of local snowfall out of the watershed. Although the export area is larger than the import area,
 283 snowfall is higher along the WRR crest. Thus, Torrey Creek imports 6.6% of its accumulation and
 284 only exports 2.8%, producing a net gain of 1.6 cm watershed-average SWE.

285 The difference between snowshed and watershed boundaries is most pronounced at
 286 smaller scales. About 23% of snow accumulation in the Continental Glacier first-order stream
 287 catchment originates outside the topographic watershed, which is a lower bound that assumes
 288 a maximal contribution from direct snowfall on the glacier (Section 2.4). The effective
 289 catchment area more than doubles (2.0 to 4.4 km²) when including areas that contribute >1%
 290 of local snowfall (Figure 4). The patch of modeled snowfall export from the Continental Glacier
 291 aligns with observed bare ice patches caused by early ablation of the thin residual snowpack
 292 (VanLooy et al., 2013).

293 There is a considerable flux of snow across the Continental Divide from Pacific to
 294 Atlantic basins (~3x10⁵ kg/m seasonally). The total mass imported into Torrey Creek (largely

295 across the Continental Divide) is $3.5 \times 10^{-3} \text{ km}^3$, equivalent to 7% of the 2024 water yield. Over
296 the October-May accumulation season, this equates to a mean snow transport flux of $0.17 \text{ m}^3/\text{s}$
297 entering the watershed, or 32% of mean streamflow on the same time period. Baker (1946)
298 first hypothesized that snow drifting across the Continental Divide might underlie patterns of
299 glacier abundance in the WRR. The present results support a sizable impact of interbasin snow
300 transport on watershed-scale snow accumulation patterns.

301 3.4 Sensitivity and Interpretation

302 The baseline 2 km moving average snowfall pattern provides a conservative lower
303 bound on transport by preserving considerable heterogeneity in the local snowfall pattern.
304 With the alternative snowfall patterns (Section 2.2.2), the contributing distance for cells with
305 SWE $>3 \text{ m}$ increases by 17-41% and the interbasin flux into Torrey Creek increases by 24-53%
306 (Table S1). While the true transport flux remains uncertain, multi-kilometer transport is an
307 important control on snow accumulation patterns in all scenarios. The relationships between
308 topography, SWE, contributing distance, and snowshed boundaries also remain reasonably
309 consistent (Figure S6-S8).

310 Minimizing Q_{dist} (Section 2.3.2) causes each snow parcel to move directly towards its
311 final destination, unlike real-world blowing snow, which is turbulent and undirected. Again, this
312 approach leads to a conservative lower bound on contributing distances since the modeled
313 snow “knows” where to go, unlike real snow.

314 It is challenging to separate transport into preferential deposition and redistribution,
315 and these results might partially represent near-surface snowfall dynamics. However, my
316 treatment is similar to process-based transport models that account for preferential deposition
317 by re-suspending snowfall after it reaches the ground (cf. Reynolds et al., 2021, Section 6.4).
318 Scipi3n et al. (2013) confirm that snowfall several hundred meters above ground is much
319 smoother than ground snow accumulation patterns. Transport fluxes described here are best
320 interpreted relative to snowfall above the near-surface flow field (Mott et al., 2018).

321 Although physically constrained by mass conservation and flux continuity, the NN is
322 highly abstracted and lacks sublimation processes. However, self-limiting humidity feedbacks
323 may reduce alpine sublimation to $\sim 0.1\%$ of precipitation (Groot Zwaaftink et al., 2013). Qu3no
324 et al. (2024) similarly found that transport outweighs sublimation in shaping landscape-scale
325 alpine snow patterns. Still, future work could potentially include sublimation in the
326 differentiable modeling framework.

327 4 Conclusions

328 Assuming that precipitation patterns are considerably smoother, the WRR snowpack
329 distribution results from multi-kilometer transport. Extensive areas of SWE $>3 \text{ m}$ (3-9 times
330 seasonal snowfall) imply contributing distances of 0.3-2.1 km with drift source areas up to 3.5
331 km^2 . Due to large interbasin transport fluxes, snowsheds may be more relevant than purely
332 topographic watersheds for understanding streamflow generation in windy and snowy
333 environments.

334 The framework described here is an example of differentiable modeling, a burgeoning
335 field in the geosciences (Shen et al., 2023). The structure of neural networks makes them well-
336 suited for representing directional transport, which could extend to many other hydrological
337 processes.

338 **Acknowledgements**

339 I acknowledge ownership of Mountain Hydrology LLC, which funded snow data
340 acquisition under Bureau of Reclamation award R24AC00025-00. I am grateful to my PhD
341 committee and especially Adrian Harpold and Mark Wigmosta for years of modeling guidance
342 and encouragement on my side projects.

343 **Open Research**

344 Data, processing scripts, and DHSVM model source code necessary to reproduce figures
345 and numerical results from this study are publicly archived at Boardman (2024a). In addition to
346 inclusion in the archive (Boardman 2024a), the modified version of DHSVM used for this study
347 is also developed publicly on GitHub (Boardman, 2024b). Lidar and hyperspectral data products
348 acquired commercially by Airborne Snow Observatories, Inc. (ASO) are excluded from the
349 archive due to contractual license restrictions but can be publicly accessed from the ASO data
350 portal (Airborne Snow Observatories, 2024).

351 **References**

352 Abatzoglou, J. T. (2013). Development of gridded surface meteorological data for
353 ecological applications and modelling. *International Journal of Climatology*, 33(1), 121–131.
354 <https://doi.org/10.1002/joc.3413>

355 Adok, U. (1977). Snow Drift. *Journal of Glaciology*, 19(81), 123–139.
356 <https://doi.org/10.3189/S0022143000215591>

357 Airborne Snow Observatories, Inc. (2024).
358 *ASO_NorthernWindRivers_2024May31_AllData_and_Reports* [Dataset].
359 <https://data.airbornesnowobservatories.com/>

360 Anderson, R. S. (2002). Modeling the tor-dotted crests, bedrock edges, and parabolic
361 profiles of high alpine surfaces of the Wind River Range, Wyoming. *Geomorphology*, 46(1–2),
362 35–58. [https://doi.org/10.1016/S0169-555X\(02\)00053-3](https://doi.org/10.1016/S0169-555X(02)00053-3)

363 Baker, C. L. (1946). Geology of the Northwestern Wind River Mountains, Wyoming.
364 *Geological Society of America Bulletin*, 57(6), 565–596. [https://doi.org/10.1130/0016-7606\(1946\)57\[565:GOTNWR\]2.0.CO;2](https://doi.org/10.1130/0016-7606(1946)57[565:GOTNWR]2.0.CO;2)

366 Baydin, A. G., Pearlmutter, B. A., Radul, A. A., & Siskind, J. M. (2017). Automatic
367 differentiation in machine learning: A survey. *J. Mach. Learn. Res.*, 18(1), 5595–5637.

368 Bennett, A., Hamman, J., & Nijssen, B. (2020). MetSim: A Python package for estimation
369 and disaggregation of meteorological data. *Journal of Open Source Software*, 5(47), 2042.
370 <https://doi.org/10.21105/joss.02042>

- 371 Boardman, E. (2024a). *Dataset for Snow Transport Modeling in the Northern Wind River*
372 *Range* [Dataset]. Zenodo. <https://doi.org/10.5281/zenodo.14201720>
- 373 Boardman, E. (2024b). *Eli-mtnhydro/DHSVM-MtnHydro* [Software].
374 <https://github.com/eli-mtnhydro/DHSVM-MtnHydro>
- 375 Calvet, M., Gunnell, Y., & Farines, B. (2015). Flat-topped mountain ranges: Their global
376 distribution and value for understanding the evolution of mountain topography.
377 *Geomorphology*, 241, 255–291. <https://doi.org/10.1016/j.geomorph.2015.04.015>
- 378 Caterini, A. L., & Chang, D. E. (2018). *Deep Neural Networks in a Mathematical*
379 *Framework*. Springer International Publishing. <https://doi.org/10.1007/978-3-319-75304-1>
- 380 Dozier, J. (2011). Mountain hydrology, snow color, and the fourth paradigm. *Eos*,
381 *Transactions American Geophysical Union*, 92(43), 373–374.
382 <https://doi.org/10.1029/2011EO430001>
- 383 Dozier, J., Bair, E. H., & Davis, R. E. (2016). Estimating the spatial distribution of snow
384 water equivalent in the world's mountains. *WIREs Water*, 3(3), 461–474.
385 <https://doi.org/10.1002/wat2.1140>
- 386 Earth Resources Observation And Science (EROS) Center. (2017). *National Agriculture*
387 *Imagery Program (NAIP), images: M_4310943_ne_12_060_20220710 and*
388 *m_4310943_nw_12_060_20220717* [Tiff]. U.S. Geological Survey.
389 <https://doi.org/10.5066/F7QN651G>
- 390 Emmerich, M., Deutz, A., & Klinkenberg, J.-W. (2008). The computation of the expected
391 improvement in dominated hypervolume of Pareto front approximations. *Leiden Institute for*
392 *Advanced Computer Science*. [https://liacs.leidenuniv.nl/~emmerichmtm/moda/material/TR-](https://liacs.leidenuniv.nl/~emmerichmtm/moda/material/TR-Exl.pdf)
393 [Exl.pdf](https://liacs.leidenuniv.nl/~emmerichmtm/moda/material/TR-Exl.pdf)
- 394 Farinotti, D., Magnusson, J., Huss, M., & Bauder, A. (2010). Snow accumulation
395 distribution inferred from time-lapse photography and simple modelling. *Hydrological*
396 *Processes*, 24(15), 2087–2097. <https://doi.org/10.1002/hyp.7629>
- 397 Groot Zwaaftink, C. D., Löwe, H., Mott, R., Bavay, M., & Lehning, M. (2011). Drifting
398 snow sublimation: A high-resolution 3-D model with temperature and moisture feedbacks.
399 *Journal of Geophysical Research: Atmospheres*, 116(D16).
400 <https://doi.org/10.1029/2011JD015754>
- 401 Groot Zwaaftink, C. D., Mott, R., & Lehning, M. (2013). Seasonal simulation of drifting
402 snow sublimation in Alpine terrain. *Water Resources Research*, 49(3), 1581–1590.
403 <https://doi.org/10.1002/wrcr.20137>
- 404 Hiemstra, C. A., Liston, G. E., & Reiners, W. A. (2006). Observing, modelling, and
405 validating snow redistribution by wind in a Wyoming upper treeline landscape. *Ecological*
406 *Modelling*, 197(1), 35–51. <https://doi.org/10.1016/j.ecolmodel.2006.03.005>
- 407 Hoffman, M. J., Fountain, A. G., & Achuff, J. M. (2007). 20th-century variations in area of
408 cirque glaciers and glacierets, Rocky Mountain National Park, Rocky Mountains, Colorado, USA.
409 *Annals of Glaciology*, 46, 349–354. <https://doi.org/10.3189/172756407782871233>

- 410 Jackson, T. H. R. (1994). *A spatially distributed snowmelt-driven hydrologic model*
 411 *applied to the upper Sheep Creek watershed* [PhD Dissertation, Department of Civil and
 412 Environmental Engineering, Utah State University]. [https://www.proquest.com/dissertations-](https://www.proquest.com/dissertations-theses/spatially-distributed-snowmelt-driven-hydrologic/docview/304120742/se-2)
 413 [theses/spatially-distributed-snowmelt-driven-hydrologic/docview/304120742/se-2](https://www.proquest.com/dissertations-theses/spatially-distributed-snowmelt-driven-hydrologic/docview/304120742/se-2)
- 414 Kingma, D. P., & Ba, J. (2017). *Adam: A Method for Stochastic Optimization*
 415 (arXiv:1412.6980). arXiv. <https://doi.org/10.48550/arXiv.1412.6980>
- 416 Komarov, A. A. (1954). Some rules on the migration and deposition of snow in Western
 417 Siberia and their application to control measures (G. Belkov, Trans.). In *Technical Translation*
 418 *(National Research Council of Canada): Vol. NRC-TT-1094* (NRC-TT-1094,). National Research
 419 Council of Canada. <https://doi.org/10.4224/20331553>
- 420 LANDFIRE. (2022). *LANDFIRE 2022 Existing Vegetation Type (EVT)* [Dataset]. U.S.
 421 Department of the Interior, Geological Survey, and U.S. Department of Agriculture.
 422 <http://www.landfire/viewer>
- 423 Lehning, M., Löwe, H., Ryser, M., & Raderschall, N. (2008). Inhomogeneous precipitation
 424 distribution and snow transport in steep terrain. *Water Resources Research*, *44*(7).
 425 <https://doi.org/10.1029/2007WR006545>
- 426 Li, D., Wrzesien, M. L., Durand, M., Adam, J., & Lettenmaier, D. P. (2017). How much
 427 runoff originates as snow in the western United States, and how will that change in the future?
 428 *Geophysical Research Letters*, *44*(12), 6163–6172. <https://doi.org/10.1002/2017GL073551>
- 429 Litaor, M. I., Williams, M., & Seastedt, T. R. (2008). Topographic controls on snow
 430 distribution, soil moisture, and species diversity of herbaceous alpine vegetation, Niwot Ridge,
 431 Colorado. *Journal of Geophysical Research: Biogeosciences*, *113*(G2).
 432 <https://doi.org/10.1029/2007JG000419>
- 433 Luce, C. H., Tarboton, D. G., & Cooley, K. R. (1998). The influence of the spatial
 434 distribution of snow on basin-averaged snowmelt. *Hydrological Processes*, *12*(10–11), 1671–
 435 1683. [https://doi.org/10.1002/\(SICI\)1099-1085\(199808/09\)12:10<1671::AID-](https://doi.org/10.1002/(SICI)1099-1085(199808/09)12:10<1671::AID-HYP688>3.0.CO;2-N)
 436 [HYP688>3.0.CO;2-N](https://doi.org/10.1002/(SICI)1099-1085(199808/09)12:10<1671::AID-HYP688>3.0.CO;2-N)
- 437 Marsh, C. B., Lv, Z., Vionnet, V., Harder, P., Spiteri, R. J., & Pomeroy, J. W. (2024).
 438 Snowdrift-Permitting Simulations of Seasonal Snowpack Processes Over Large Mountain
 439 Extents. *Water Resources Research*, *60*(8), e2023WR036948.
 440 <https://doi.org/10.1029/2023WR036948>
- 441 Marsh, C. B., Pomeroy, J. W., Spiteri, R. J., & Wheeler, H. S. (2020). A Finite Volume
 442 Blowing Snow Model for Use With Variable Resolution Meshes. *Water Resources Research*,
 443 *56*(2), e2019WR025307. <https://doi.org/10.1029/2019WR025307>
- 444 McGrath, D. (2022). Blowing in the wind: The glaciers of Colorado. *Mountain Geologist*,
 445 *59*(3), 229–238. <https://doi.org/10.31582/rmag.mg.59.3.229>
- 446 Mott, R., & Lehning, M. (2010). Meteorological Modeling of Very High-Resolution Wind
 447 Fields and Snow Deposition for Mountains. *Journal of Hydrometeorology*, *11*(4), 934–949.
 448 <https://doi.org/10.1175/2010JHM1216.1>

- 449 Mott, R., Schirmer, M., Bavay, M., Grünewald, T., & Lehning, M. (2010). Understanding
 450 snow-transport processes shaping the mountain snow-cover. *The Cryosphere*, 4(4), 545–559.
 451 <https://doi.org/10.5194/tc-4-545-2010>
- 452 Mott, R., Scipión, D., Schneebeli, M., Dawes, N., Berne, A., & Lehning, M. (2014).
 453 Orographic effects on snow deposition patterns in mountainous terrain. *Journal of Geophysical*
 454 *Research: Atmospheres*, 119(3), 1419–1439. <https://doi.org/10.1002/2013JD019880>
- 455 Mott, R., Vionnet, V., & Grünewald, T. (2018). The Seasonal Snow Cover Dynamics:
 456 Review on Wind-Driven Coupling Processes. *Frontiers in Earth Science*, 6.
 457 <https://doi.org/10.3389/feart.2018.00197>
- 458 Musselman, K. N., Pomeroy, J. W., Essery, R. L. H., & Leroux, N. (2015). Impact of
 459 windflow calculations on simulations of alpine snow accumulation, redistribution and ablation.
 460 *Hydrological Processes*, 29(18), 3983–3999. <https://doi.org/10.1002/hyp.10595>
- 461 Naaim-Bouvet, F., Bellot, H., & Naaim, M. (2010). Back analysis of drifting-snow
 462 measurements over an instrumented mountainous site. *Annals of Glaciology*, 51(54), 207–217.
 463 <https://doi.org/10.3189/172756410791386661>
- 464 Olyphant, G. A. (1985). Topoclimate and the Distribution of Neoglacial Facies in the
 465 Indian Peaks Section of the Front Range, Colorado, U.S.A. *Arctic and Alpine Research*, 17(1), 69–
 466 78. <https://doi.org/10.1080/00040851.1985.12004449>
- 467 Outcalt, S. I., & MacPhail, D. D. (1965). A Survey of Neoglaciation in the Front Range of
 468 Colorado. *University of Colorado Studies, Series in Earth Sciences*, 4, 124.
- 469 Painter, T. H., Berisford, D. F., Boardman, J. W., Bormann, K. J., Deems, J. S., Gehrke, F.,
 470 Hedrick, A., Joyce, M., Laidlaw, R., Marks, D., Mattmann, C., McGurk, B., Ramirez, P.,
 471 Richardson, M., Skiles, S. M., Seidel, F. C., & Winstral, A. (2016). The Airborne Snow
 472 Observatory: Fusion of scanning lidar, imaging spectrometer, and physically-based modeling for
 473 mapping snow water equivalent and snow albedo. *Remote Sensing of Environment*, 184, 139–
 474 152. <https://doi.org/10.1016/j.rse.2016.06.018>
- 475 Paszke, A., Gross, S., Massa, F., Lerer, A., Bradbury, J., Chanan, G., Killeen, T., Lin, Z.,
 476 Gimelshein, N., Antiga, L., Desmaison, A., Köpf, A., Yang, E., DeVito, Z., Raison, M., Tejani, A.,
 477 Chilamkurthy, S., Steiner, B., Fang, L., ... Chintala, S. (2019). *PyTorch: An Imperative Style, High-*
 478 *Performance Deep Learning Library* (arXiv:1912.01703). arXiv.
 479 <https://doi.org/10.48550/arXiv.1912.01703>
- 480 Pomeroy, J. W., Gray, D. M., & Landine, P. G. (1993). The Prairie Blowing Snow Model:
 481 Characteristics, validation, operation. *Journal of Hydrology*, 144(1), 165–192.
 482 [https://doi.org/10.1016/0022-1694\(93\)90171-5](https://doi.org/10.1016/0022-1694(93)90171-5)
- 483 Quéno, L., Mott, R., Morin, P., Cluzet, B., Mazzotti, G., & Jonas, T. (2024). Snow
 484 redistribution in an intermediate-complexity snow hydrology modelling framework. *The*
 485 *Cryosphere*, 18(8), 3533–3557. <https://doi.org/10.5194/tc-18-3533-2024>

- 486 Reynolds, D. S., Pflug, J. M., & Lundquist, J. D. (2021). Evaluating Wind Fields for Use in
 487 Basin-Scale Distributed Snow Models. *Water Resources Research*, 57(2), e2020WR028536.
 488 <https://doi.org/10.1029/2020WR028536>
- 489 Rigge, M. B., Bunde, B., Shi, H., & Postma, K. (2021). *Rangeland Condition Monitoring*
 490 *Assessment and Projection (RCMAP) Fractional Component Time-Series Across the Western U.S.*
 491 *1985-2020* [Dataset]. U.S. Geological Survey. <https://doi.org/10.5066/P95IQ4BT>
- 492 Schneiderbauer, S., & Prokop, A. (2011). The atmospheric snow-transport model:
 493 SnowDrift3D. *Journal of Glaciology*, 57(203), 526–542.
 494 <https://doi.org/10.3189/002214311796905677>
- 495 Scipión, D. E., Mott, R., Lehning, M., Schneebeli, M., & Berne, A. (2013). Seasonal small-
 496 scale spatial variability in alpine snowfall and snow accumulation. *Water Resources Research*,
 497 49(3), 1446–1457. <https://doi.org/10.1002/wrcr.20135>
- 498 Shen, C., Appling, A. P., Gentine, P., Bandai, T., Gupta, H., Tartakovsky, A., Baity-Jesi, M.,
 499 Fenicia, F., Kifer, D., Li, L., Liu, X., Ren, W., Zheng, Y., Harman, C. J., Clark, M., Farthing, M., Feng,
 500 D., Kumar, P., Aboelyazeed, D., ... Lawson, K. (2023). Differentiable modelling to unify machine
 501 learning and physical models for geosciences. *Nature Reviews Earth & Environment*, 4(8), 552–
 502 567. <https://doi.org/10.1038/s43017-023-00450-9>
- 503 Sturm, M. (2015). White water: Fifty years of snow research in WRR and the outlook for
 504 the future. *Water Resources Research*, 51(7), 4948–4965.
 505 <https://doi.org/10.1002/2015WR017242>
- 506 Sun, N., Yan, H., Wigmosta, M. S., Leung, L. R., Skaggs, R., & Hou, Z. (2019). Regional
 507 Snow Parameters Estimation for Large-Domain Hydrological Applications in the Western United
 508 States. *Journal of Geophysical Research: Atmospheres*, 124(10), 5296–5313.
 509 <https://doi.org/10.1029/2018JD030140>
- 510 Tabler, R. D. (1971). Design of a Watershed Snow Fence System, and First-Year Snow
 511 Accumulation. *Proceedings of the 39th Annual Western Snow Conference*, 50–55.
- 512 Tabler, R. D., & Schmidt, R. A. (1973). Weather conditions that determine snow
 513 transport distances at a site in Wyoming. In *The role of snow and ice in hydrology* (Vol. 1, pp.
 514 118–127). Proceedings of the Banff Symposia.
- 515 Vandenberg, G. S., & VanLooy, J. A. (2016). Continental Glacier meltwater contributions
 516 to late summer stream flow and water quality in the northern Wind River Range, Wyoming,
 517 USA. *Environmental Earth Sciences*, 75(5), 389. <https://doi.org/10.1007/s12665-016-5295-0>
- 518 VanLooy, J. A., Forster, R. R., Barta, D., & Turrin, J. (2013). Spatially variable surface
 519 elevation changes and estimated melt water contribution of Continental Glacier in the Wind
 520 River Range, Wyoming, USA: 1966–2011. *Geocarto International*, 28(2), 98–113.
 521 <https://doi.org/10.1080/10106049.2012.665500>
- 522 VanLooy, J. A., & Vandenberg, G. S. (2024). Glacier Meltwater Impacts to Late Summer
 523 Flow and Geochemistry of Tributaries in the Wind River Range, Wyoming, USA. *The Professional*
 524 *Geographer*, 0(0), 1–7. <https://doi.org/10.1080/00330124.2024.2341073>

- 525 Viviroli, D., Dürr, H. H., Messerli, B., Meybeck, M., & Weingartner, R. (2007). Mountains
526 of the world, water towers for humanity: Typology, mapping, and global significance. *Water*
527 *Resources Research*, 43(7). <https://doi.org/10.1029/2006WR005653>
- 528 Vögeli, C., Lehning, M., Wever, N., & Bavay, M. (2016). Scaling Precipitation Input to
529 Spatially Distributed Hydrological Models by Measured Snow Distribution. *Frontiers in Earth*
530 *Science*, 4. <https://doi.org/10.3389/feart.2016.00108>
- 531 Wagenbrenner, N. S., Forthofer, J. M., Page, W. G., & Butler, B. W. (2019). Development
532 and Evaluation of a Reynolds-Averaged Navier–Stokes Solver in WindNinja for Operational
533 Wildland Fire Applications. *Atmosphere*, 10(11), Article 11.
534 <https://doi.org/10.3390/atmos10110672>
- 535 Walter, B., Huwald, H., Gehring, J., Bühler, Y., & Lehning, M. (2020). Radar
536 measurements of blowing snow off a mountain ridge. *The Cryosphere*, 14(6), 1779–1794.
537 <https://doi.org/10.5194/tc-14-1779-2020>
- 538 Wang, Z., & Huang, N. (2017). Numerical simulation of the falling snow deposition over
539 complex terrain. *Journal of Geophysical Research: Atmospheres*, 122(2), 980–1000.
540 <https://doi.org/10.1002/2016JD025316>
- 541 Wigmore, O., & Molotch, N. P. (2024). Snow drifts as a driver of alpine plant productivity
542 as observed from weekly multispectral drone imagery. *Ecohydrology*, 17(7), e2694.
543 <https://doi.org/10.1002/eco.2694>
- 544 Wigmosta, M. S., Vail, L. W., & Lettenmaier, D. P. (1994). A distributed hydrology-
545 vegetation model for complex terrain. *Water Resources Research*, 30(6), 1665–1679.
546 <https://doi.org/10.1029/94WR00436>
- 547 Williams, C. J., McNamara, J. P., & Chandler, D. G. (2009). Controls on the temporal and
548 spatial variability of soil moisture in a mountainous landscape: The signature of snow and
549 complex terrain. *Hydrology and Earth System Sciences*, 13(7), 1325–1336.
550 <https://doi.org/10.5194/hess-13-1325-2009>
- 551